

## 5.3 Consumer Responses to Price Changes: Substitution and Income Effects

### Substitution Effect

- the change in a consumer's consumption choices that results from a change in the relative prices of two goods.

↗  
Utility held constant!  
(on same indifference curve)

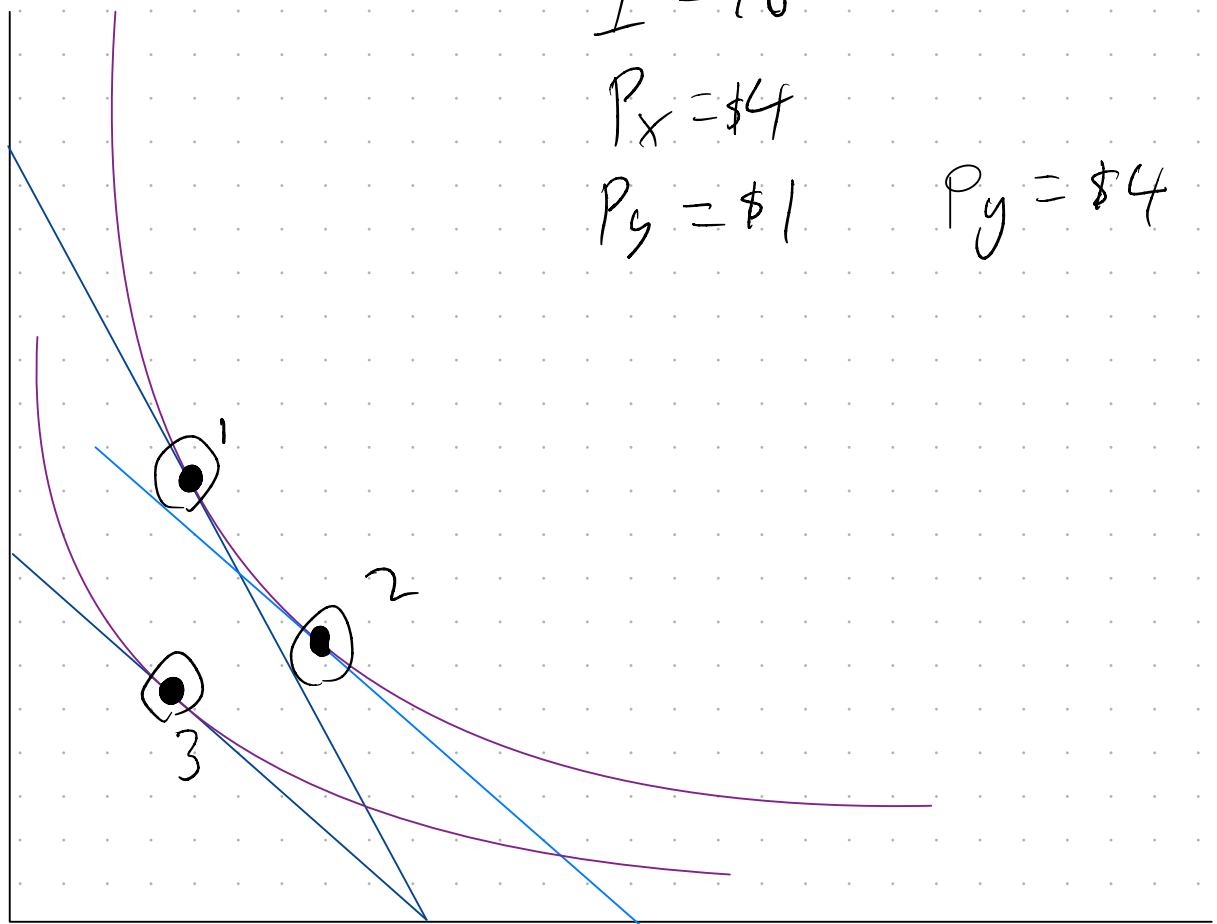
### Income Effect

- the change in a consumer's consumption choices that results

from a change in the purchasing power of the consumer's income.

(Purchasing Power Effect)

↑ relative prices held constant,  
only purchasing power affected



$$I = 16$$

$$P_x = \$4$$

$$P_y = \$1$$

$$P_y = \$4$$

1 → 2  
Sub. Effect

2 → 3  
Income effect

Total Effect = Substitution Effect + Income Effect

Q. What is the sub. Effect and the Income Effect when  $P_y \uparrow$  from 1 to 4?

$$U(x, y) = xy$$

$$MRS_{xy} = \frac{y}{x}$$

$$P_x = 4 \quad I = 16$$

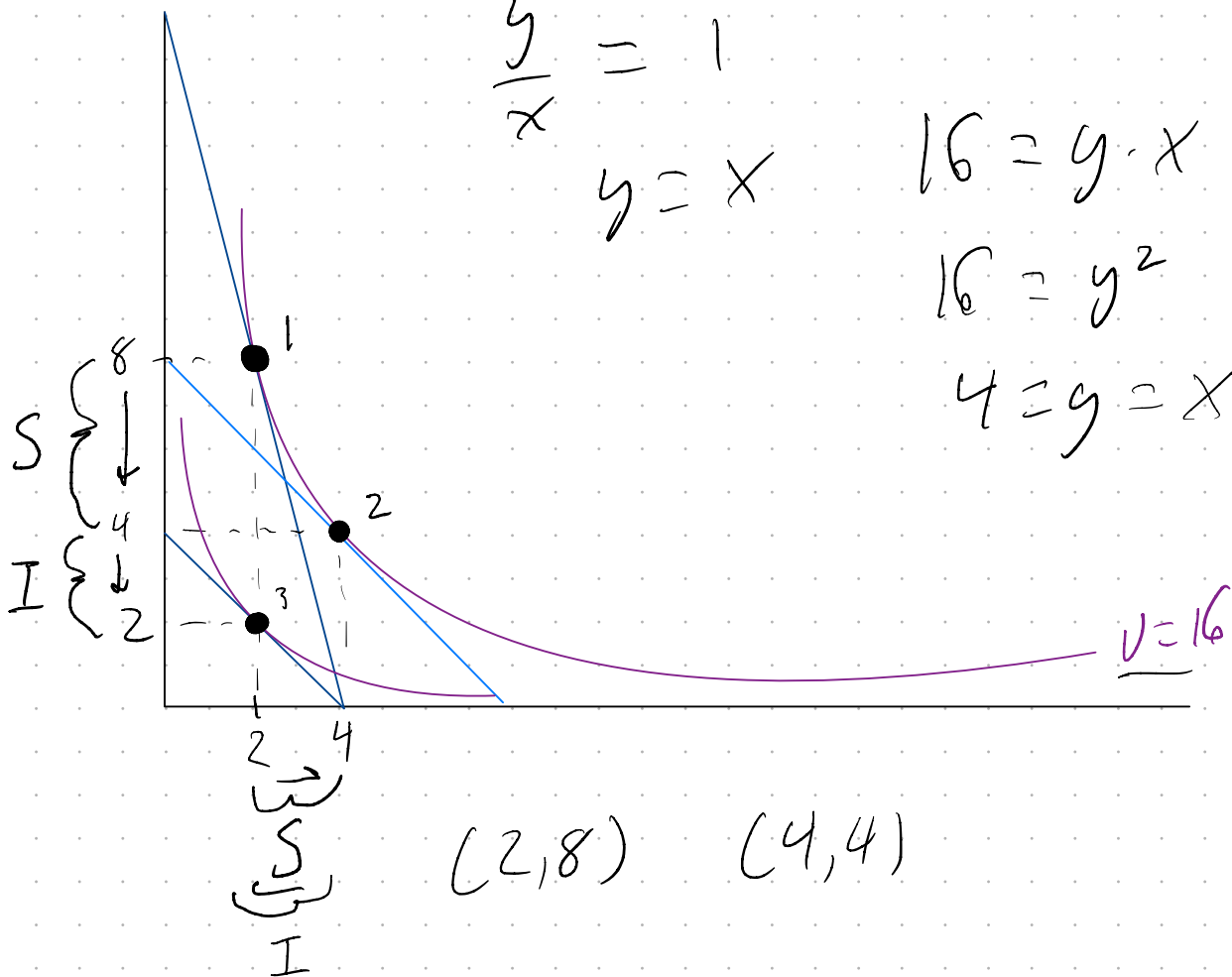
$$P_y = 1, \quad P_y = 4$$

$$\frac{y}{x} = 1$$
$$y = x$$

$$16 = y \cdot x$$

$$16 = y^2$$

$$4 = y = x$$



1. Find original bundle
2. Find slope of new budget line
3. Set  $MRS = \text{slope of new line}$
4. System of Eq. with old utility level
5. Calculate difference in  $x, y$  from 1 to 2.  
This is the substitution effect.

To find the income effect

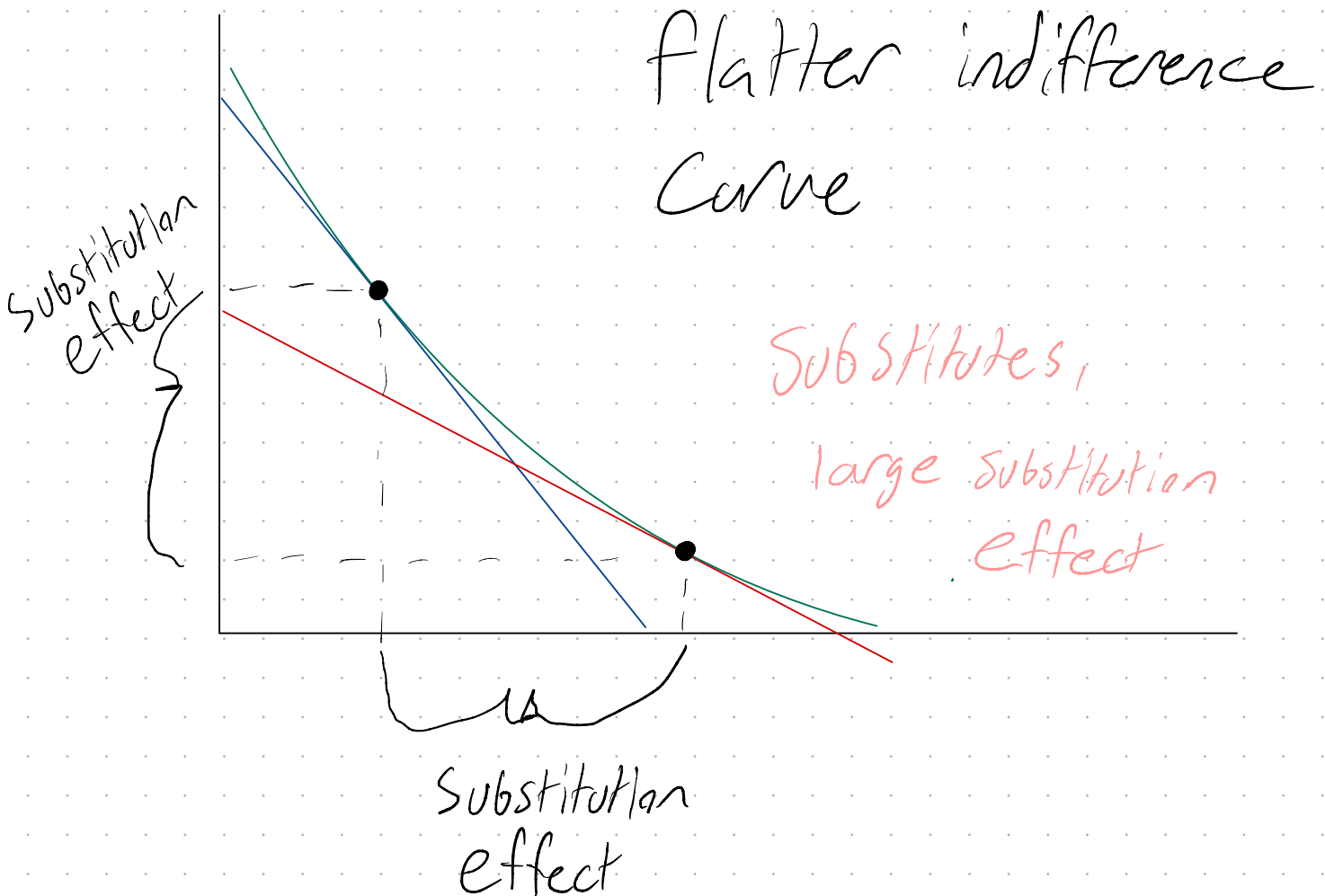
do steps above then

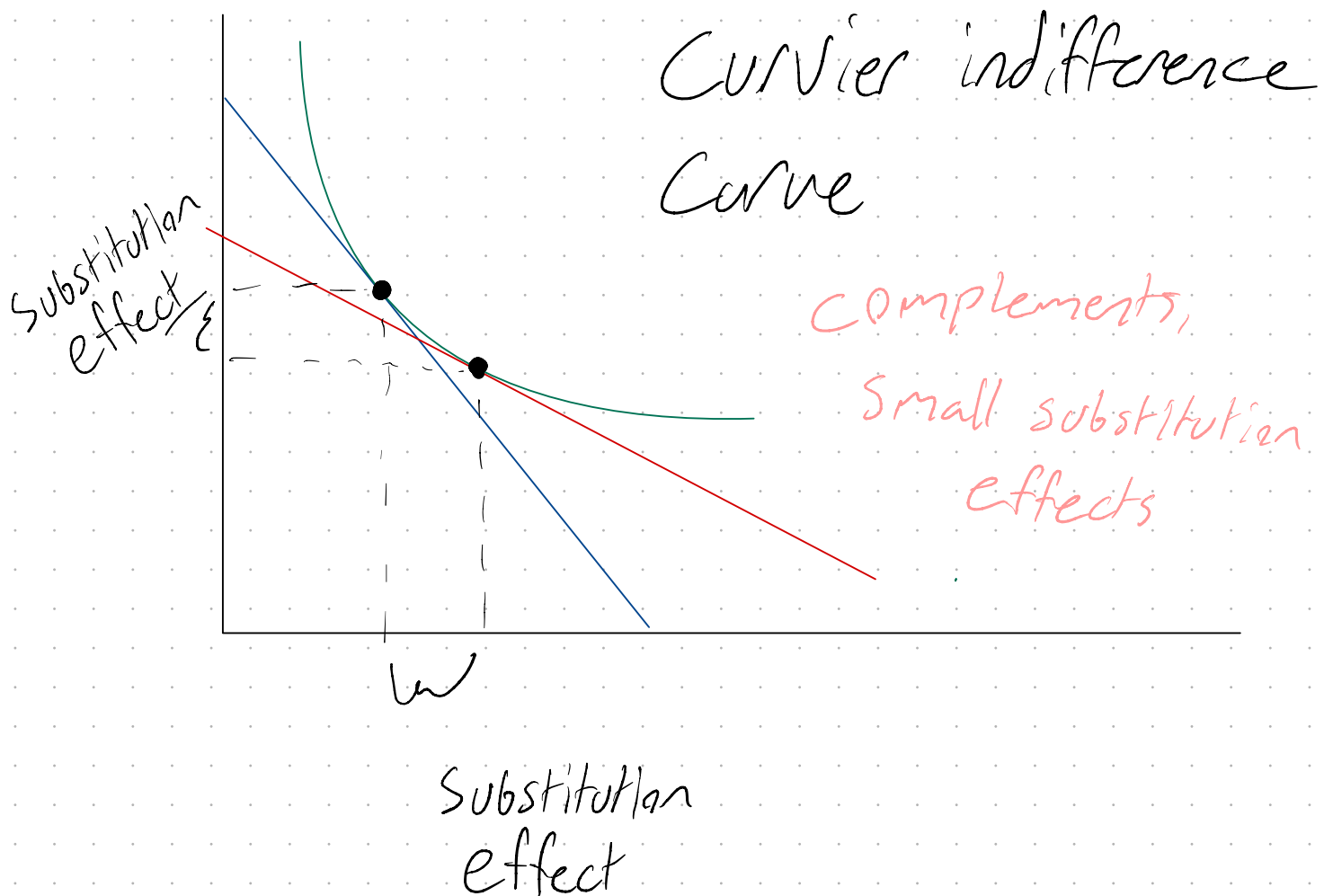
6. Find point 3, the new optimal bundle under the new prices.
7. Calculate the difference in  $x, y$  from 2 to 3. This is the income effect.

Q: What determines the size of the substitution + Income Effects?

## Substitution Effect

- Depends on the curvature of indifference curves





## Income effect

- Depends on how much was consumed of the good whose price changed.

ex: originally consumed 10 units of good X.  $P_x \downarrow$  by \$5. Now effective income  $\uparrow$  by \$50.

# Income and Substitution effects for inferior goods

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$X$  &  $Y$  both normal  
not perfect sub/complements

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$P_x \uparrow$

Substitution Effects

$Q_x \downarrow$

$Q_y \uparrow$

Income Effects

$Q_x \downarrow$

$Q_y \downarrow$

Total Effect

$Q_x \downarrow$   $Q_y ?$

$X$  inferior,  $y$  normal  
not perfect sub/complements

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$P_x \downarrow$

Substitution Effects

$Q_x \uparrow$

$Q_y \downarrow$

Income Effects

$Q_x \downarrow$

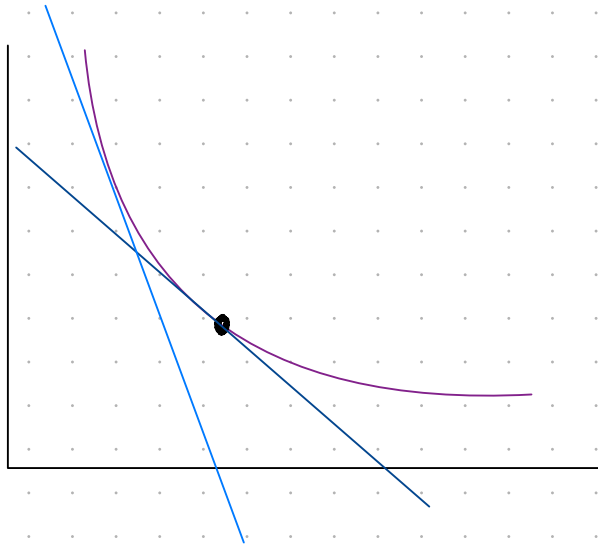
$Q_y \uparrow \uparrow$

Total Effect

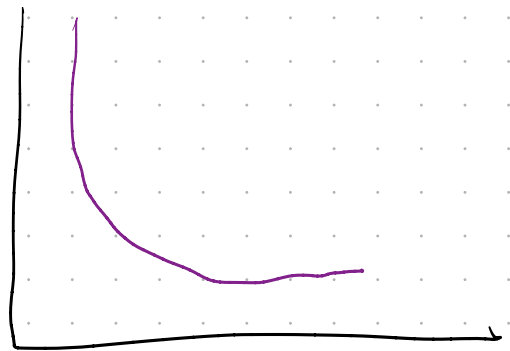
$Q_x ?$   $Q_y \uparrow (?)$

$\nearrow$

Q: If  $P_x \uparrow$  is the substitution effect always  $Q_x \downarrow, Q_y \uparrow$ ?  
not perfect sub/complements



4. Indifference curves are  
convex to the origin  
(curve away)

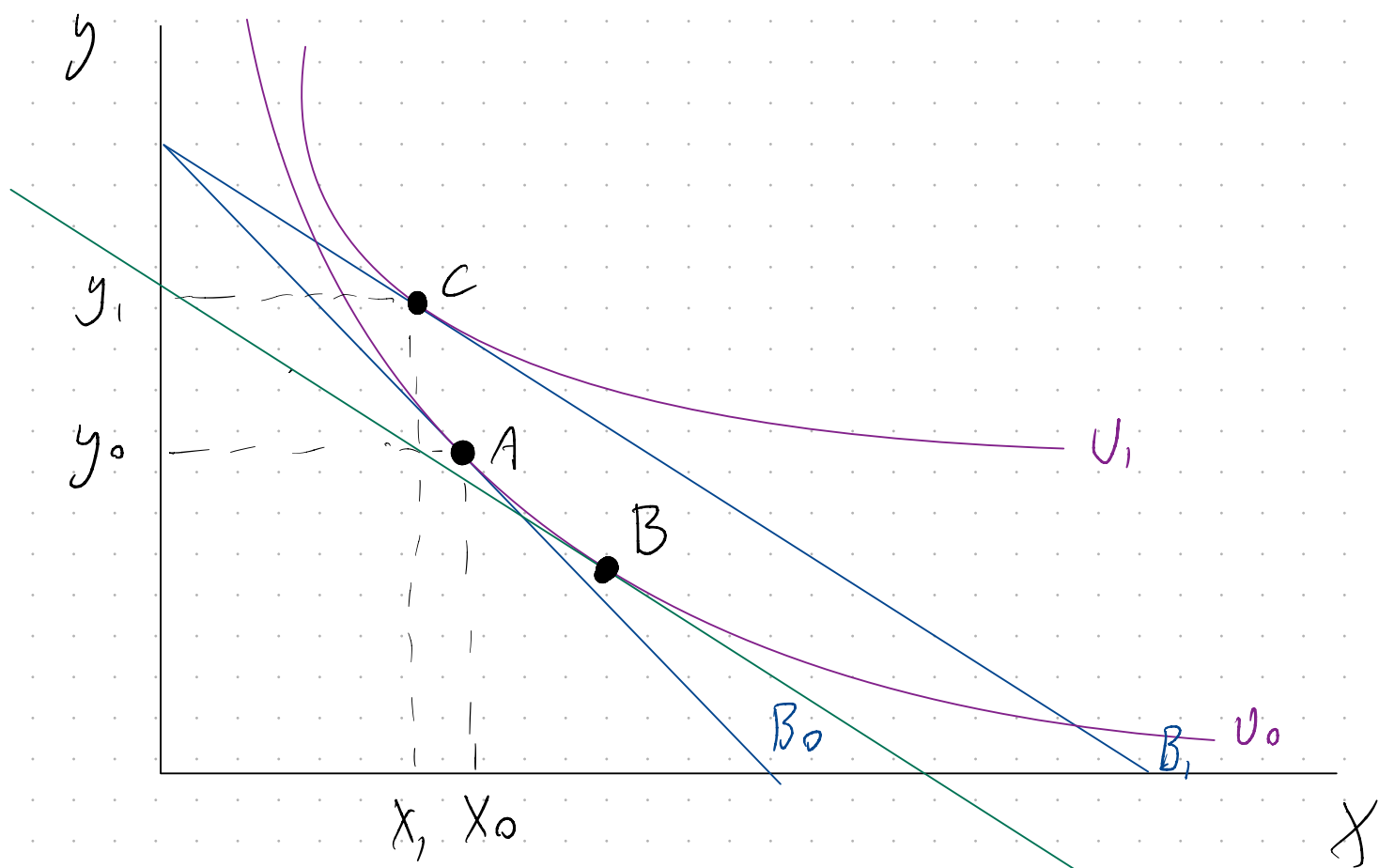




# Giffin Goods:

goods where when  $P_x \downarrow$ ,  $Q_x \downarrow$ .

$P_x \downarrow$



$A \rightarrow B$  : substitution effect

$B \rightarrow C$  : Income effect

Q: Why must giffen goods be inferior goods?

Need:  $P_x \downarrow \rightarrow Q_x \downarrow$

2 effects:

Substitution

Income

↓

↓

$$\Delta Q_x^{Sub} \geq 0$$

need

$$\Delta Q_x^{Sub} + \Delta Q_x^{Inc} < 0$$

↑

always

$$\Delta Q_x^{Inc} < -\Delta Q_x^{Sub}$$

$$-\Delta Q_x^{Sub} \leq 0$$

$$\Delta Q_x^{Inc} < -\Delta Q_x^{Sub} \leq 0$$

$$\Delta Q_x^{Inc} < 0$$

↗  
This is a

Inferior good

5.4: The Impact of Changes  
in another good's price: Substitutes  
and complements

Substitutes: goods that can  
be used in place  
of one another

Assume  $X, Y$  are substitutes.

$P_x \downarrow$

Sub.  
effect  
 $Q_y \downarrow$

Income  
effect

$Q_y \uparrow$

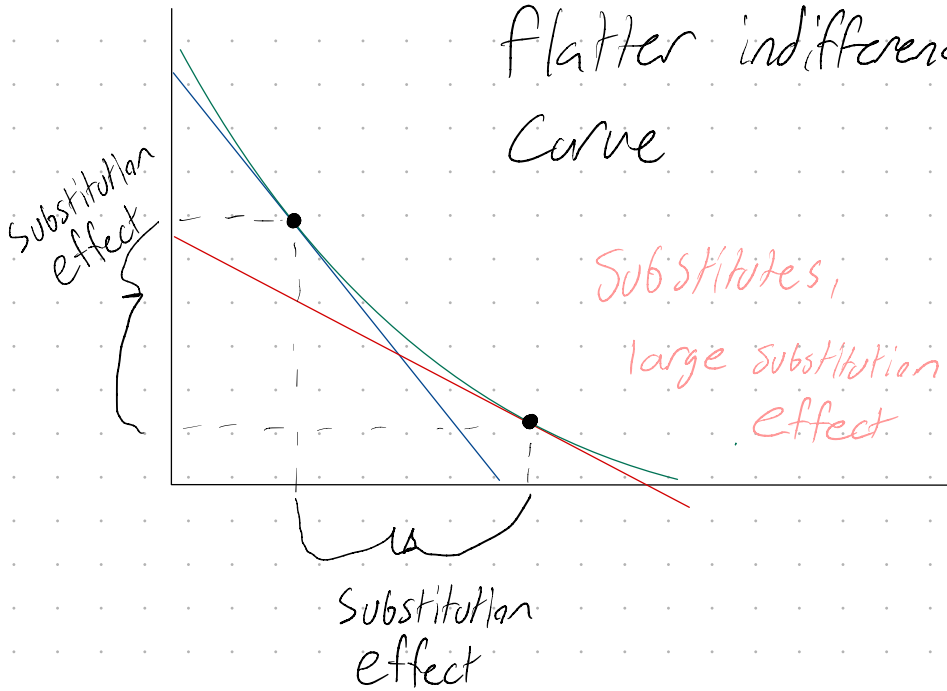
$P_x \uparrow$

Sub.  
effect  
 $Q_y \uparrow$

Income  
effect

$Q_y \downarrow$

What effect dominates?



flatter indifference  
curve

Sub. Effect

Large

Dominates

income effect

Total Effect

$Q_y \downarrow$

Total Effect

$Q_y \uparrow$

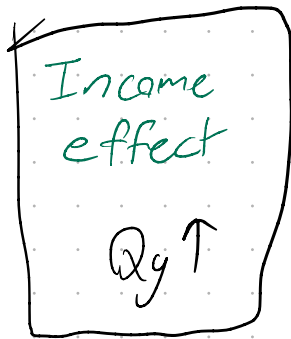
Complements: goods that are used in combination

Assume  $X$  &  $Y$  are complements

$P_x \downarrow$

Sub. effect

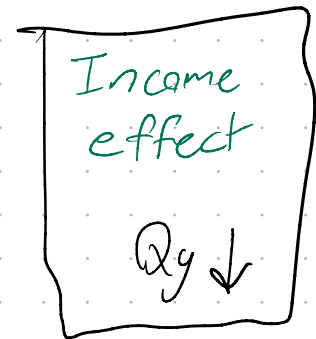
$Q_y \downarrow$



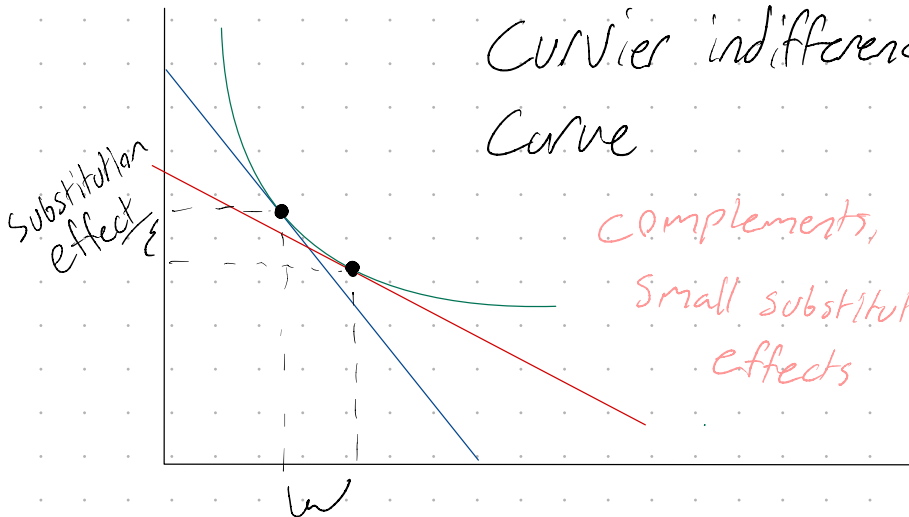
$P_x \uparrow$

Sub. effect

$Q_y \uparrow$



What effect dominates?



Convex indifference curve

Complements,  
Small substitution effects

Sub. effect is small

Income effect dominates

Substitution effect  
Total Effect

$Q_y \uparrow$

Total Effect

$Q_y \downarrow$